Naval Research Laboratory

Stennis Space Center, MS 39529-5004





NRL/FR/7240--94-9618

Semi-Automated Mesoscale Analysis System, Version 1.2: Evaluation Test Results

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Remote Sensing Applications Branch Remote Sensing Division

September 28, 1995

19951002 032

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REPORT DOCUMENTATION PAGE

Form Approved OBM No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.

| 1. AGENCY USE ONLY (Leave blank) | 2. REPORT DATE | 3. REPORT TYPE AND DAT | ES COVERED | |
|--|---|--|-------------------------------|-----------------------|
| | September 28, 1995 | Final | | |
| 4. TITLE AND SUBTITLE | | 1. | FUNDING NUMBER | |
| Semi-Automated Mesoscale Analysis | System, Version 1.2: Evaluation | Test Results | lob Order No. | 572519705 |
| | | P | Program Element No. | 0603207N |
| 6. AUTHOR(S) | | P | Project No. | X1596 |
| | .: | 7 | ask No. | |
| Matthew Lybanon and Sarah H. Peck | anpaugn | l _A | Accession No. | DN394464 |
| | | | DEDECRING OF | CANIZATION |
| 7. PERFORMING ORGANIZATION NAME(S) | AND ADDRESS(ES) | 8 | PERFORMING ORCE REPORT NUMBER | |
| Naval Research Laboratory | | | | |
| Remote Sensing Division | 14 | | NRL/FR/7240 | 94-9618 |
| Stennis Space Center, MS 39529-500 | 14 | | | |
| 9. SPONSORING/MONITORING AGENCY NAI | ME(S) AND ADDRESS(ES) | 1 | 0. SPONSORING/MO | NITORING |
| Space and Naval Warfare Systems Co | | | AGENCY REPORT | NUMBER |
| SPAWAR 005 | | | | |
| Washington, D.C. 20363-5100 | | | | |
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| 11. SUPPLEMENTARY NOTES | | | | |
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| 12a. DISTRIBUTION/AVAILABILITY STATEM | ENT | 1 | 2b. DISTRIBUTION C | ODE |
| Sie i i i i e i i e i e i e i e i e i e | | | | |
| Approved for public release; distribution | ution unlimited | | | |
| Approved for public release; distribu | mon unimited. | | | |
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| of the latter. | Mark Mark Control | • | | |
| 14. SUBJECT TERMS | | | 15. NUMB | ER OF PAGES |
| | | | | 19 |
| satellite remote sensing, expert syste | em, artificial intelligence, automa | ted analysis | 16. PRICE | CODE |
| | | | | |
| 17. SECURITY CLASSIFICATION | 18. SECURITY CLASSIFICATION OF THIS PAGE | 19. SECURITY CLASSIFICA OF ABSTRACT | ATION 20. LIMITA | ATION OF ABSTRACT |
| OF REPORT Unclassified | Unclassified | Unclassified | s | Same as report |

Unclassified

Unclassified

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EXECUTIVE SUMMARY

The Naval Research Laboratory's Remote Sensing Applications Branch has developed the Semi-Automated Mesoscale Analysis System (SAMAS), a prototype image analysis system for satellite images of the Gulf Stream region. Previous tests demonstrated that SAMAS shows rudimentary skill in automatically locating the Gulf Stream and its associated eddies. Since those tests, SAMAS has been updated in several ways. This report describes the performance of SAMAS Version 1.2, a newer version that incorporates some new techniques, as well as improvements to some old ones.

SAMAS 1.2 was tested by applying it to a set of 22 warmest-pixel composite multichannel sea surface temperature (MCSST) images covering February through June 1993, which were also analyzed by a human expert. The human analyses were regarded as "truth" for the purposes of the statistical analysis of the test results. The human analyses are subjective combinations of analyses from the Naval Oceanographic Office's Warfighting Support Center and information from inspection of the composite images. The analyses, both human and automated, include North Wall positions and eddy definitions, center position coordinates, and sizes.

The statistical analysis consists of tabulations and accuracy measures. For eddies, the tabulations compare the number of eddies found by SAMAS versus the number found by the analyst, and the locations and sizes of the eddies. Accuracy measures include position errors and size fractional errors, their first- and second-order statistics (means and standard deviations), as well as minimum and maximum values. The Gulf Stream statistical results were obtained using the same software that was used to evaluate the Gulfcast and Data Assimilation Research and Transition (DART) numerical models. Statistics include information on the longitude range spanned by each Gulf Stream determination, mean position errors, and first- and second-order statistics of the latter.

SAMAS 1.2 showed some improvement over the earlier version. It found over 80% of the rings the analyst found, with a mean position error of approximately 22 km and a mean fractional size error of 0.165. Gulf Stream mean position errors were in the range of 40-45 km. Gulf Stream statistics were not available for the earlier version, so a comparison is not possible.

SEMI-AUTOMATED MESOSCALE ANALYSIS SYSTEM, VERSION 1.2: EVALUATION TEST RESULTS

1.0 INTRODUCTION

Infrared (IR) satellite images of the ocean provide surface temperature measurements which can be used either to supplement local measurements at various depths obtained by conventional oceanographic techniques or to provide information about areas of the ocean where data from conventional techniques are sparse. Since satellite IR images often depict mesoscale features clearly, the use of such imagery for various oceanographic applications is expanding rapidly. However, present interpretive techniques are largely manual, require significant effort, and are both subjective in nature and highly dependent upon the interpreter's skill. With the proliferation of oceanographic analyses that use satellite data, combined with decreasing Navy manpower levels, it becomes highly desirable for certain applications to move from labor-intensive manual interpretation toward a capability for automated image interpretation.

Over the past several years the Naval Research Laboratory's (NRL) Remote Sensing Applications Branch has developed a prototype image analysis system that shows rudimentary skill in automatically locating both the Gulf Stream and eddies in IR images of the Gulf Stream region. The system is known as the Semi-Automated Mesoscale Analysis System (SAMAS). Some early results are given by Holyer and Peckinpaugh (1990). Since that earlier report, continuing development of old techniques, plus the addition of some new ones, have resulted in significant changes to SAMAS.

This report describes evaluation tests of the latest version of SAMAS, Version 1.2, and provides a statistical analysis of the test results. To clarify some of the details, an outline of the processing approach that SAMAS employs is presented here. It is helpful to think of three levels of analysis. The lowest level consists of operations that focus on individual image pixels, without taking advantage of any contextual information. SAMAS' lowest level performs image segmentation. Segmentation is the step that divides an image into regions, which in some cases are objects in the images. Segmentation, in general, can be edge-based or region-based. The output of the lowest level is, therefore, either a set of edges or a set of regions (the regions are bounded by the edges). SAMAS uses an edge-based segmenter known as the cluster shade edge detector (Holyer and Peckinpaugh 1989).

The detected edges are passed to an intermediate level which performs two functions, labeling and feature synthesis. Labeling consists of assigning oceanographic identities to the edge fragments created by the segmenter. Feature synthesis combines edge fragments with identical labels into continuous features, at the same time calculating associated parameters such as position and radius. (These two steps could be accomplished with region fragments, but SAMAS 1.2 uses an edge segmenter.) The labeling and feature synthesis functions are a mixture of conventional image processing and artificial intelligence, i.e., some algorithms are pixel-based and some are object-oriented and use contextual information. SAMAS 1.2 offers a choice of two labelers. One is based on nonlinear probabilistic relaxation (Krishnakumar et al. 1990) and one is based on the topography of the image brightness function considered as a surface (Krishnamurthy et al. 1993). The feature

synthesis module for the Gulf Stream uses an expansion of the North Wall in empirical orthogonal functions (EOF) or principal components (Molinelli and Flanigan 1987). That for warm and cold rings fits circles using the circular Hough transform (Duda and Hart 1972).

The highest level consists of an expert system that describes the kinematics of mesoscale features using rules about the time evolution of eddies (both translational motion and size changes) and a neural network that forecasts the coefficients of the EOF expansion at a later time (Thomason 1989; Chase and Holyer 1993; Lybanon 1994). The expert system has two main functions in SAMAS. First, the forecast feature positions can provide approximate feature locations during periods of cloud cover, when direct observation is not possible. Second, the expert system can "update" feature positions from a previous analysis to provide a better first guess for the relaxation labeler.

2.0 SAMAS AUTOMATED PROCESSING

The test images are a set of MCSST warmest-pixel composites that cover the period February through June 1993. Each composite consists of one to four images, spanning a 1- to 5-day period. A cloud mask was computed for each image, and a composite cloud mask was created from the individual cloud masks for each of the test images. The method used to create the cloud mask was developed by Gallegos et al. (1993) (see Fig. 1a for an example MCSST warmest-pixel composite image with cloud mask). We acquired the oceanographic analyses for the north Atlantic Ocean covering the test period from the Warfighting Support Center (WSC) of the Naval Oceanographic Office (NAVOCEANO). The analyses include North Wall positions and eddy definitions, center position coordinates, and sizes. The actual days of the WSC analyses do not correspond exactly with the dates of our image data (see Table 1 for image dates and Fig. 2 for WSC dates). For each of the composite images, a human analyst created a subjective analysis consisting of North Wall positions and eddy definitions, based on the composite image and WSC analyses for the composite image time span. These will be referred to as the human analysis.

The first step of the automated processing is edge creation, using the cluster shade edge detector (Holyer and Peckinpaugh 1989). The window size for computing the gray-level co-occurrence (GLC) matrix used to compute the image of cluster shade values is 16 x 16 pixels, and the delta x and y values are zero. For every overlapping 16- x 16-pixel window of the image, a cluster shade value is computed. Using these values, edges are defined. The zero-crossing test is performed as follows: For every overlapping 3- x 3-pixel window of the image containing the cluster shade values, an initial zero-crossing test for the cluster shade values is done. If within the window there is a value greater than 200 and another value less than -200, an edge is found. The edge is denoted by a value of one at the location of the window's center in the output binary edge image, to be referred to henceforth as the edge image. Once this initial test is done, multiple passes are made through the cluster shade image to extend these edges (up to 30 passes or when no new edges are found). Next, for every overlapping 3- x 3-pixel window of the cluster shade image, a test is performed. If the center pixel is not already marked as an edge, and any of the other pixels in the window are edge pixels, then the cluster shade values of the window are tested. If there is a value greater than 100 and another value less than -100, an edge is found and thus marked in the edge image.

The last step in the creation of the edge image is a cleaning step. For every overlapping $16-\times 16$ -pixel window of the edge image, the following test is performed. If the border of the window has no edge marked, but edge points are contained within the window, then the window is "cleaned," i.e., edge pixels are set to zero (see Fig. 1b for an example edge image).

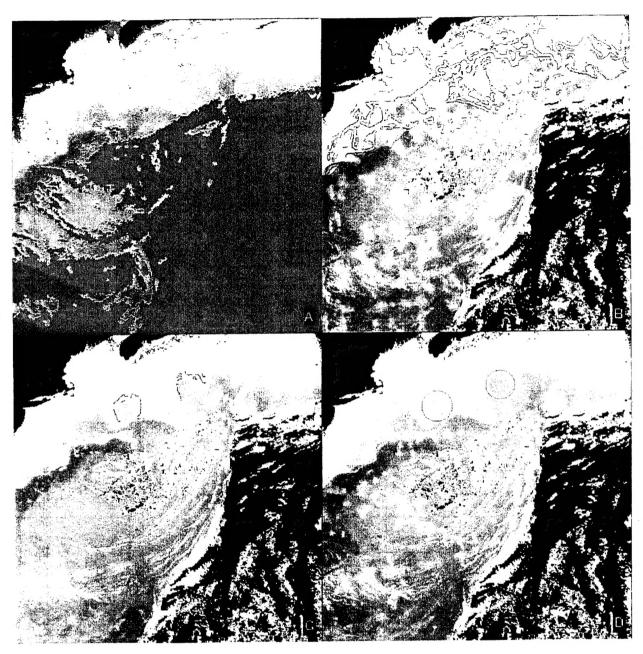


Fig. 1 — (a) MCSST warmest-pixel composite for April 20-24 with composite cloud mask displayed over the image; (b) cluster shade edges displayed over the image; (c) relaxation-labeled edges displayed over the image (yellow for Gulf Stream North Wall edges, red for eddy edges); and (d) CEOF North Wall displayed in yellow, Hough eddies displayed in blue

At this point we have the test image, cloud mask, edges, and human analysis for each of the 22 cases. For edge labeling, the test image, cloud mask, and a previous analysis are needed. With the exception of the first image (in temporal sequence), the previous analysis will be the human analysis from the previous image. For the first image, a WSC analysis will serve as the previous analysis. The next step is to propagate the previous analysis forward in time to match the current image time. The oceanographic expert system accomplishes this task (Lybanon 1990). The expert system depicts expected motions and size changes of warm- and cold-core rings, and their interaction with each other and with the Gulf Stream in the northwest Atlantic Ocean. The

Table 1 — Dates of Images Used for MCSST Warmest Composites. Notice that Some Composites Contain Multiple Images from a Single Day.

| No. | Date Range | Images | Used to Cr | eate Comp | posite |
|-----|--------------|--------|------------|-----------|--------|
| 1 | Mar 1–2 | Mar 1 | Mar 2 | Mar 2 | |
| 2 | Mar 812 | Mar 8 | Mar 8 | Mar 12 | |
| 3 | Mar 1216 | Mar 12 | Mar 16 | | |
| 4 | Mar 2123 | Mar 21 | Mar 23 | | |
| 5 | Mar 28-31 | Mar 28 | Mar 28 | Mar 31 | |
| 6 | Mar 31-Apr 4 | Mar 31 | Apr 2 | Apr 4 | |
| 7 | Apr 4–7 | Apr 4 | Apr 6 | Apr 7 | |
| 8 | Apr 7–11 | Apr 7 | Apr 10 | Apr 11 | Apr 11 |
| 9 | Apr 18–20 | Apr 18 | Apr 19 | Apr 20 | |
| 10 | Apr 20-24 | Apr 20 | Apr 24 | | |
| 11 | Apr 24–26 | Apr 24 | Apr 26 | Apr 26 | Apr 26 |
| 12 | May 8-10 | May 8 | May 9 | May 9 | May 10 |
| 13 | May 9-12 | May 9 | May 9 | May 10 | May 12 |
| 14 | May 16–19 | May 16 | May 17 | May 18 | May 19 |
| 15 | May 27-28 | May 27 | May 28 | | |
| 16 | May 28-30 | May 28 | May 30 | | |
| 17 | Jun 2-5 | Jun 2 | Jun 5 | Jun 5 | |
| 18 | Jun 9-12 | Jun 9 | Jun 12 | | |
| 19 | Jun 13-14 | Jun 13 | Jun 14 | | |
| 20 | Jun 16 | Jun 16 | Jun 16 | | |
| 21 | Jun 21 | Jun 21 | | | |
| 22 | Jun 26-27 | Jun 26 | Jun 27 | | |

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| S | M | Tu | W | Th | F | 3 | 3 | | | | | | 6 |
| 1 | 2 | 3 | 4 | 5 | 6 | | | 1 | 2 | 3 | 4 | 5 | |
| 7 | 8 | 9 | 10 | 11 | 12 | 13 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| 14 | 15 | 16 | 17 | 18 | 19 | 20 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 21 | 22 | 23 | 24 | 25 | 26 | 27 |
| 28 | | | | | | | 28 | 29 | 30 | 31 | | | |
| | | Ap | ril 19 | 993 | | | | | M | ay 199 | 93 | | |
| s | M | Tu | W | Th | F | S | s | M | Tu | W | Th | F | S |
| | | | | 1 | 2 | 3 | | | | | | | 1 |
| 4 | 5 | 6 | 7 | 8 | 9 | 10 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 18 | 19 | 20 | 21 | 22 | 23 | 24 | 16 | 17 | 18 | 19 | 20 | 21 | 22 |
| 25 | 26 | 27 | 28 | 29 | 30 | | 23 | 24 | 25 | 26 | 27 | 28 | 29 |
| | | | | | | | 30 | 31 | | | | | |
| | | Ju | ne 19 | 93 | | | | | | | | | |
| s | M | Tu | W | Th | F | S | | | | | | | |
| | | 1 | 2 | 3 | 4 | 5 | | | | | | | |
| 6 | 7 | 8 | 9 | 10 | 11 | 12 | | | | | | | |
| 13 | 14 | 15 | 16 | 17 | 18 | 19 | | | | | | | |
| 20 | 21 | 22 | 23 | 24 | 25 | 26 | | | | | | | |
| 27 | 28 | 29 | 30 | | | | | | | | | | ' |

Fig. 2 — Days for WSC analyses (marked bold)

domain is divided into nine regions. The rules that describe the expected behavior of the warm- and cold-core rings differs in each region. For each ring in the analysis, the expert system calculates a new size and center position at a later time. The expert system progresses the Gulf Stream's North Wall in time using a trained neural network rather than rules (Chase and Holyer 1993). Refer to Table 2 for the number of days that the previous analyses are projected in time. Where the number of days is given as zero, the analyses were not processed by the expert system, but used "as is."

The image, corresponding cloud mask and edge image, along with the previous analysis, projected to the image time as needed, are used by the edge-labeling routine to create a new labeled edge image. There are two steps in executing the probabilistic relaxation labeling algorithm (Krishnakumar et al. 1990). In the first step, a priori probabilities are evaluated with the help of a previous, as-needed, time-projected analysis. In the second step, these a priori probabilities are iteratively updated (relaxation) until a consistent labeling is reached. The resulting labeled edge image contains zero values at no edge or discarded edges. One nonzero value is used to represent

Table 2 — Shown for Each Test Image is the Previous Analysis for Labeling Images and Filling in Missing Eddies, Along with the Number of Days Projected by the Expert System for the Analysis. Also Shown is the Previous Analysis for CEOF Modes Creation and Number of Days Projected by the Expert System. All Previous Analyses are Created by the Human Analyst Except Where Specified as WSC.

| No. | Image | Previous Analysis Used for Labeling and Eddy Fill-In for Missing Data | No. of Days Projected Forward by Expert System | Previous Analysis Used by CEOF to Create Modes | No. of Days Projected Forward by Expert System |
|-----|--------------|---|---|--|--|
| 1 | Mar 1-2 | Feb 27 (WSC) | 2 | Feb 27 (WSC) | 2 |
| 2 | Mar 8–12 | Mar 1-2 | 6 | Mar 1–2 | 6 |
| 3 | Mar 12–16 | Mar 8–12 | 0 | Mar 1–2 | 6 |
| 4 | Mar 21–23 | Mar 12–16 | 5 | Mar 12-16 | 5 |
| 5 | Mar 28–31 | Mar 21-23 | 5 | Mar 21-23 | 5 |
| 6 | Mar 31-Apr 4 | Mar 28–31 | 0 | Mar 28-31 | 0 |
| 7 | Apr 4–7 | Mar 31–Apr 4 | 0 | Mar 28-31 | 0 |
| 8 | Apr 7–11 | Apr 4–7 | 0 | Apr 4-7 | 0 |
| 9 | Apr 18–20 | Apr 7–11 | 7 | Apr 7–11 | 7 |
| 10 | Apr 20–24 | Apr 18–20 | 0 | Apr 7–11 | 7 |
| 11 | Apr 24–26 | Apr 20–24 | 0 | Apr 7–11 | 7 |
| 12 | May 8–10 | Apr 24–26 | 12 | Apr 24–26 | 12 |
| 13 | May 9–12 | May 8–10 | 0 | Apr 24–26 | 12 |
| 14 | May 16–19 | May 9–12 | 4 | May 9–12 | 4 |
| 15 | May 27–28 | May 16–19 | 8 | May 16–19 | 8 |
| 16 | May 28–30 | May 27–28 | 0 | May 27–28 | 0 |
| 17 | Jun 2-5 | May 28–30 | 2 | May 28–30 | 2 |
| 18 | Jun 9-12 | Jun 2–5 | 4 | Jun 2-5 | 4 |
| 19 | Jun 13-14 | Jun 9-12 | 1 | Jun 9-12 | 1 |
| 20 | Jun 16 | Jun 13-14 | 2 | Jun 13-14 | 2 |
| 21 | Jun 21 | Jun 16 | 5 | Jun 16 | 5 |
| 22 | Jun 26–27 | Jun 21 | 5 | Jun 21 | 5 |

the North Wall of the Gulf Stream, and a different nonzero value is assigned to each eddy (defined by edges) in the output labeled edge image. Figure 1c shows an example of a labeled edge image.

The Gulf Stream North Wall positions are extracted from the labeled image and converted from image-pixel coordinates to latitude and longitude. These positions are then input to the Complex Empirical Orthogonal Function (CEOF) module used for Gulf Stream formation (Molinelli and Flanigan 1987). The CEOF module also uses a Gulf Stream to create a mode file. This Gulf Stream must be of good quality, i.e., the full-length stepwise straight-line interpolation is believable. It is used to "prime" the formation of the current Gulf Stream. Table 2 shows images and the Gulf Stream used to create the required mode file. The number of days used by the expert system to project the human analysis forward in time is the same as that used for the labeling. When a Gulf Stream proves to be unusable for mode file creation, older previous analyses are checked until a suitable Gulf Stream is found (see Fig. 1d for an example of a CEOF-generated Gulf Stream).

The eddy edges are extracted from the labeled edge image to form an eddy edge image. These eddy edges are dilated to double width and then input to the eddy detection routine. The eddy detection uses a modified circular Hough transform (Peckinpaugh and Holyer 1994). Circular features, eddies, are defined by center x, y position and pixel radius sizes. These values are converted to latitude, longitude position and kilometer radius. The Hough transform modification biases the results toward smaller circular features. For each possible radius, an accumulator array image is created (reasonable eddy size for our region is 50–133 km). Each element in the accumulator array image contains the sum of points making up the circle at the corresponding x, y center position of the original image. These values are normalized for the number of points which define a circle of the radius size that corresponds to the accumulator array image. From a series of these accumulator array images, the best (i.e., largest) values are selected. These values define the center position and size values assigned to the eddy. A test is performed to eliminate overlapping of eddies. The test uses a minimum threshold so that 40% of the circle must be defined to detect an eddy. Figure 1d shows an example of Hough transform-defined eddies.

Due to cloud cover in the image, some eddies may not be visible or be defined by clear edges. For this reason, the Hough transform eddies are combined with eddies from the previous analysis. The eddies from the previous analysis, progressed in time by the expert system as needed, are used to fill in eddies not defined by the Hough transform (see Table 2 for previous analysis definitions). A zero value in the "No. of days projected forward by Expert System" column means that no expert system was used for that case. Hough transform eddies are given first priority where there is any overlap with the previous analysis eddies. This combined eddy list defines the eddies for the current image (see Fig. 1d for an example of automated analysis). Note that all eddies for this case were created by the Hough transform.

3.0 STATISTICAL ANALYSIS

3.1 SAMAS vs. Human Analysis Eddies

The test data set consisted of 22 images. However, the human expert did not find eddies in nine of the images, so the SAMAS tests employed 13 images for which the analyst found one or more eddies. Let E = the number of eddies found by the expert in one image, and let S = E + N = the number of eddies found by SAMAS in one image. Table 3 shows the values of N for the 13 cases for which the expert found at least one eddy.

Table 3 — Number of Occurrences of Each Value of the Difference N Between the Number of Eddies Found by SAMAS and the Number Found by the Human Expert

| N | Number of Images |
|------------|------------------|
| - 7 | 1 |
| | ••• |
| -5 | 1 |
| | ••• |
| -2 | 3 |
| -1 | 2 |
| 0 | 4 |
| +1 | 2 |

Note: For N = 0, in some cases the SAMAS-found eddies and the analyst-found eddies were not the same eddies (i.e., there were significant differences in their geographical positions).

There were two cases in which (apparently) the same eddy could be tracked over an extended period, and there were significant discrepancies between the expert and SAMAS values of both position and size. Those two cases are tabulated in Table 4. The abbreviations used in the "Sources" columns in the table are as follows: EE = eddy editor, OC = (NAVOCEANO) Operational Oceanography Center, ED = edge detector, and ES = expert system.

Table 5 gives the position and size errors for each date interval. In the table, "ground truth" values are those found by a human analyst, and "comparison" values are from SAMAS.

3.2 Gulf Stream Error Analysis

3.2.1 Means of Evaluation

SAMAS-produced Gulf Stream North Walls are compared with those produced by a human analyst using a program developed by Geraldine Gardner of Harvard University, originally for use in evaluating the Harvard Gulfcast model. The two Gulf Streams are compared over a specified longitude range by interpolating each to a standard grid. The error is estimated by calculating the area between them and dividing that area by the arc length of the ground truth Gulf Stream

segment within that longitude range, so that the result is a mean error expressed in kilometers. That program was modified slightly by Dan Fox, and further modified by Matthew Lybanon (both of NRL) to read the SAMAS-format Gulf Stream files. However, the "core" subroutine that performs the error calculation (and other routines called by it) was unchanged, except for one change (by Fox) to compensate for the different sizes of a degree of latitude and a degree of longitude. The original Harvard code failed to compensate for this difference.

The program was set up to perform the calculation over four longitude ranges. That feature was retained and used as described below. The program also requires the data—both ground truth (analyst) and comparison (SAMAS) files—to span the longitude range used in the calculation. Since each file covered a generally different longitude range, in many cases it was necessary to extrapolate the files so that they spanned the largest longitude range used in the analysis. Table 6 illustrates that extrapolation. The left side of the table lists the original longitude limits in each file, and the right side gives the limits after the extrapolation. In every case except one, the method used was linear extrapolation based on the first two or last two points in the file. The exception was for the June 21 "analyst" Gulf Stream, which was very short. It was necessary to extrapolate the western end from -59.8077° to -80.0° (a distance greater than the original length). Two points resulting from a linear least-squares fit to the first six points in the original file were necessary to obtain reasonable results.

The most straightforward approach is to compare all the cases over the same longitude ranges. However, it was not clear that this approach was advisable because of the large variations between the longitude ranges actually covered by the different data sets (shown in Table 6). The approach adopted for the analysis is a compromise. The four longitude ranges used in the analysis were split into two pairs of ranges. Two "global" ranges, the same for all data sets, make up the first pair.

Table 4 — Two Cases for Which There were Significant Differences Between SAMAS-Derived and Expert-Derived Eddies

| | | | Eddy | A | 1 | | |
|--------------|---------|-----------|---------|-----------|-------------|--------|-------|
| | G | round Tru | th | Er | rors | Sou | irces |
| Dates | Lat. | Lon. | Rad. | Pos. (km) | Fract. Size | Expert | SAMAS |
| 24-26 Apr 93 | 39.1454 | -68.419 | 61.5132 | 62.25707 | -0.01714 | EE | ES |
| 16-19 May 93 | 39.5446 | -68.651 | 39.2824 | 41.49992 | -0.01143 | EE | ES |
| 27-28 May 93 | 39.4251 | -69.910 | 46.9616 | 66.62056 | 0.373079 | EE | ED |
| 28-30 May 93 | 39.3852 | -69.885 | 47.2837 | 20.10504 | 0.732155 | EE | ED |
| 2-5 Jun 93 | 39.2854 | -69.910 | 45.6201 | 13.71933 | 0.743262 | EE | ED |
| 13-14 Jun 93 | 39.3652 | -70.347 | 44.7902 | 20.70246 | 0.539013 | EE | ED |
| | | | Means: | 37.48406 | 0.393157 | | |
| | | | Eddy | В | | | |
| | G | round Tru | th | Er | rors | Sou | irces |
| Dates | Lat. | Lon. | Rad. | Pos. (km) | Fract. Size | Expert | SAMAS |
| 20-24 Apr 93 | 40.5100 | -65.570 | 64.8200 | 15.38535 | 0.632211 | OC | ED |
| 24-26 Apr 93 | 40.5129 | -65.617 | 73.9719 | 14.94265 | 0.231426 | EE | ED |
| 8-10 May 93 | 40.5326 | -65.180 | 37.1211 | 83.69115 | 0.764086 | EE | ED |
| 9–12 May 93 | 40.4737 | -65.180 | 37.4276 | 35.02390 | 0.632581 | EE | ED |
| 16-19 May 93 | 40.5914 | -65.566 | 66.7426 | 19.09353 | 0.015390 | EE | ED |
| 27-28 May 93 | 40.1391 | -66.106 | 60.6521 | 0 | 0 | EE | EE |
| 28-30 May 93 | 40.0404 | -66.183 | 71.4185 | 12.96360 | -0.000570 | EE | ES |
| 13-14 Jun 93 | 40.1588 | -65.951 | 51.5543 | 24.70246 | 0.539013 | EE | ED |
| 16 Jun 93 | 40.2377 | -66.209 | 48.4476 | 34.42538 | -0.001430 | EE | ES |
| | | | Means: | 26.69200 | 0.312523 | | |

Notes: (Eddy B) For the 27-28 May 93 data, both the expert and SAMAS values were input by the eddy editor, so they were identical.

(Both eddies) In almost every case, the edge detector found bigger eddies than the expert. This was also true for other eddies in the test cases.

Table 5 -- Comparison of SAMAS-Derived Eddies with Those Found by Human Expert

| 1 | 5 | Ground Truth | h | | Comparison | u | | |
|--------------|--------------------------------------|--|--------------------------------------|--------------------------------------|--|--------------------------------------|---|--|
| Dates | Lat. | Lon. | Rad. | Lat. | Lon. | Rad. | Position Error (km) | Size Fract. Error |
| Mar 1-2 | None | | | | | | | |
| Mar 8–12 | None | | **** | | | | | |
| Mar 12–16 | None | | | | | | | |
| Mar 21–23 | None | | | | | | | |
| Mar 28–31 | None | | | | | | | |
| Mar 31-Apr 4 | None | | | | | | | |
| Apr 4–7 | None | | | | | · | | |
| Apr 7–11 | None | | | | | | | |
| Apr 18–20 | 40.552 | -65.592 -60.296 | 75.275 82.379 | None None | | | | |
| Apr 20–24 | None 40.510 41.770 | -65.570 -60.300 | 64.820 87.970 | 41.770 40.478 41.743 | -60.300 -65.393 -60.228 | 87.970 105.800 97.562 | 15.385 | 0.632 |
| Apr 24–26 | 39.145 40.513 41.949 37.156 | -68.419 -65.617 -60.527 -64.666 | 61.513 73.972 67.980 26.008 | 39.048 40.402 41.900 41.631 | -69.129 -65.518 -61.150 -60.552 | 60.459 91.091 67.864 89.414 | 62.257 –0.01 14.943 0.23 51.866 –0.00 Different Eddies | -0.0171 0.231 -0.00171 Eddies |
| May 8–10 | 40.533 | -65.180 -60.682 | 37.121 63.578 | 40.593 41.738 | -66.167 -60.682 | 65.485 | 83.692 0 | 0.764 |
| | 36.578 | -64.692 | 22.986 | 36.578 | -64.692 | 22.986 | 0 0 | 000 |
| | 39.245 None | -52.661 | 55.334 | 39.245 39.209 | -52.661 -69.985 | 55.334 | 0 | Ð |

Table 5 — Continued

| | g | Ground Truth | 41 | C | Comparison | | | |
|-----------|--|---|--|--|---|--|---|--|
| Dates | Lat. | Lon. | Rad. | Lat. | Lon. | Rad. | Position Error (km) | Size Fract. Error |
| May 9–12 | 41.661 40.474 38.259 36.474 | -60.887 -65.180 -63.278 -64.820 | 60.114 37.428 21.210 24.471 | 41.644 40.764 None None | -61.094 | 60.080 | 17.287 35.024 | -0.00057 0.633 |
| May 16–19 | 39.545 40.591 41.660 33.060 38.502 36.016 | -68.651 -65.566 -61.299 -74.152 -62.995 | 39.282 66.743 57.373 35.671 31.663 22.926 | 39.480 40.421 41.628 33.040 None None | -69.127 -65.593 -61.555 -74.596 | 38.834 67.770 55.343 35.589 | 41.500 19.094 21.592 41.484 | $\begin{array}{c} -0.0114 \\ 0.0154 \\ -0.0354 \\ -0.00228 \end{array}$ |
| May 27–28 | 39.425 35.807 40.139 41.235 38.522 | -69.910 -66.106 -62.250 -56.260 | 46.962 32.983 60.652 70.113 33.916 | 39.403 35.807 40.139 41.235 38.522 | -69.136 -66.106 -66.106 -62.250 -56.260 | 64.482 32.983 60.652 70.113 33.916 | 66.621 0 0 0 0 | 0.373 0 0 0 0 |
| May 28–30 | 39.385 40.040 41.196 35.786 39.105 | -69.885 -66.183 -62.147 -66.106 -56.312 | 47.284 71.419 61.469 29.727 28.960 | 39.209 39.989 41.188 35.778 None | -69.935 -66.320 -62.250 -66.201 | 81.903 71.378 61.100 29.719 | 20.105 12.964 8.642 8.644 | 0.732 -0.00057 -0.006 -0.00029 |
| Jun 2–5 | 41.930 40.650 40.493 39.285 38.462 | -57.828 -64.203 -65.926 -69.910 -56.620 | 45.515 52.428 50.854 45.620 42.234 | 40.088 41.123 40.115 39.403 35.799 | -66.243 -62.524 -66.117 -69.960 -66.201 | 60.617 85.921 46.802 79.528 32.973 | Different Different 45.107 13.719 Different | Different Eddies Different Eddies 5.107 -0.0797 3.719 0.743 Different Eddies |
| Jun 9-12 | 41.351 40.395 | -64.075 -65.720 | 50.665 57.129 | None None | | | | |

Table 5 — Continued

| | Ð | Ground Truth | th | | Comparison | u u | | |
|-----------|--|--|--|--|---|--|--|---|
| Dates | Lat. | Lon. | Rad. | Lat. | Lon. | Rad. | Position Error (km) | Size Fract. Error |
| Jun 9-12 | 39.105 38.401 41.448 | -70.399 -57.031 -55.772 | 42.720 28.713 36.478 | None None None | | | | |
| Jun 13-14 | 39.365 40.159 41.467 41.968 38.603 | -70.347 -65.951 -63.895 -56.800 | 44.790 51.554 35.152 30.675 43.578 | 39.248 40.326 41.433 41.368 38.595 | -70.533 -65.767 -64.010 -64.096 -57.079 | 68.933 80.590 35.132 56.371 43.577 | 20.702 24.273 10.375 Different 8.643 | 0.539 0.563 -0.00057 t Eddies -0.000028 |
| Jun 16 | 42.026 41.545 40.238 38.137 | -56.903 -64.203 -66.209 -56.877 | 29.546 47.014 48.448 41.843 | None 41.424 40.110 38.117 | -63.721 -66.551 -57.123 | 66.753 48.378 41.840 | 42.382 32.425 21.607 | 0.420 -0.00143 -0.000072 |
| Jun 21 | None | None | | | | | | |
| Jun 26-27 | 39.644 41.795 41.968 36.764 39.185 39.225 38.360 | -66.311 -63.869 -57.057 -67.237 -59.319 -56.517 | 59.217 47.623 33.089 51.917 65.070 31.732 | None None None None None | | | | |
| | | | | | | Mean Std. Dev. Min. Max. | 21.972 21.573 0 83.691 | 0.165 0.278 -0.0797 0.764 |

Note 1 – All dates are in 1993.

Note 2 – Eddy center latitude and longitude are in degrees; eddy radius is in kilometers.

Note 3 – A "different eddies" notation means that the "comparison" data set did not contain an eddy corresponding to the one in the "ground truth" data set; the one listed is the comparison eddy closest to the ground truth eddy.

Table 6—Gulf Stream File Longitude Limits

| | | Original | inal | | | Extrapolated | olated | |
|--------------|----------|----------|----------|----------|----------|--------------|----------|----------|
| | Ana | Analyst | SAMAS | IAS | Analyst | lyst | SAMAS | IAS |
| Date | Min. | Max. | Min. | Max. | Min. | Max. | Min. | Max. |
| Mar 8-12 | -74.8201 | -60.6303 | -80.0882 | -58.5268 | -80.0000 | -53.0000 | Same | -53.0000 |
| Mar 12-16 | -74.8458 | -67.0825 | -80.0636 | -58.4649 | -80.0000 | -53.0000 | Same | -53.0000 |
| Mar 21-23 | -74.9229 | -62.8924 | -80.0490 | -57.7529 | -80.0000 | -53.0000 | Same | -53.0000 |
| Mar 28-31 | -74.8458 | -50.5277 | -80.1636 | -57.9483 | -80.0000 | Same | Same | -53.0000 |
| Mar 31-Apr 4 | -74.9229 | -64.4091 | -74.6993 | -56.5151 | -80.0000 | -53.0000 | -80.0000 | -53.0000 |
| Apr 7–11 | -74.8972 | -50.4763 | -75.5156 | -58.2901 | -80.0000 | Same | -80.0000 | -53.0000 |
| Apr 18–20 | -74.9229 | -58.5738 | -80.1094 | -58.5272 | -80.0000 | -53.0000 | Same | -53.0000 |
| Apr 20–24 | -74.7686 | -49.6023 | -79.8836 | -58.3902 | -80.0000 | Same | -80.0000 | -53.0000 |
| Apr 24–26 | -74.8972 | -54.8721 | -80.0190 | -58.5644 | -80.0000 | -53.0000 | Same | -53.0000 |
| May 8-10 | -74.9229 | -57.3142 | -79.9709 | -58.6314 | -80.0000 | -53.0000 | -80.0000 | -53.0000 |
| May 9-12 | -74.8715 | -57.5198 | -80.4305 | -59.4863 | -80.0000 | -53.0000 | Same | -53.0000 |
| May 16-19 | -74.8972 | -56.3887 | -80.3070 | -58.2478 | -80.0000 | -53.0000 | Same | -53.0000 |
| May 27–28 | -74.8201 | -53.3297 | -80.1542 | -60.3940 | -80.0000 | -53.0000 | Same | -53.0000 |
| May 28-30 | -74.7686 | -53.8952 | -74.9946 | -57.7872 | -80.0000 | -53.0000 | -80.0000 | -53.0000 |
| Jun 2-5 | -74.8715 | -49.6280 | -79.8973 | -60.4567 | -80.0000 | Same | -80.0000 | -53.0000 |
| Jun 9-12 | -74.8458 | -50.1936 | -75.7989 | -63.6797 | -80.0000 | Same | -80.0000 | -53.0000 |
| Jun 13-14 | -74.8201 | -50.0650 | -80.0183 | -59.9915 | -80.0000 | Same | Same | -53.0000 |
| Jun 16 | -74.8715 | -51.8130 | -80.0056 | -59.9575 | -80.0000 | Same | Same | -53.0000 |
| Jun 21 | -59.8077 | -49.6280 | -79.9960 | -58.8618 | -80.0000 | Same | -80.0000 | -53.0000 |
| Jun 26-27 | -73.5605 | -53.9467 | -83.5738 | -70.0201 | -80.0000 | -53.0000 | Same | -53.0000 |

Note 1 – All dates are in 1993.

Note 2 – A "same" entry in an "extrapolated" column means that the value is the same as the one in the corresponding "original" column.

"Global 1," the longer, is -79.8° to -54.0° ; "Global 2" is -74.6° to -63.6° . The values were based on the distributions of endpoint longitudes. Table 7 shows the longitude ranges used as the second pair. They are specific to each data set. The "Special 1" range is always longer than "Special 2."

The Global 1 values were chosen so that, on the average, the SAMAS (generally longer) data ranges prior to extrapolation covered the interval. Global 2 values were chosen so that, again on the average, both SAMAS and analyst data ranges prior to extrapolation covered the interval. Hence, Global 2 is a more conservative choice. Special 1 and Special 2 values were chosen similarly, uniquely for each data set. As a result, Special 2 is a more conservative choice than Special 1.

3.2.2 Error Statistics

Table 8 shows the results of the Gulf Stream mean position errors for all four longitude ranges for each data set, as well as the overall means and standard deviations. Global 2 and Special 2 results have comparable mean values, and because of the way the ranges were chosen, the results

Table 7 — Gulf Stream Longitude Ranges Specific to Each Date ("Special" Values)

| | Special 1 | | Special 2 | |
|--------------|-----------|--------|-----------|--------|
| Date | Min. | Max. | Min. | Max. |
| Mar 8-12 | -77.5 | -59.6 | -72.2 | -61.7 |
| Mar 12-16 | -77.5 | -60.6 | -72.2 | -70.3 |
| Mar 21-23 | -77.5 | -60.3 | -72.4 | -65.5 |
| Mar 28-31 | -77.5 | -52.4 | -72.2 | -63.5 |
| Mar 31-Apr 4 | -74.8 | -60.4 | -74.4 | -68.4 |
| Apr 7–11 | -77.5 | -54.5 | -72.3 | -62.6 |
| Apr 18-20 | -77.5 | -58.55 | -72.3 | -58.60 |
| Apr 20-24 | -77.3 | -51.8 | -72.2 | -65.0 |
| Apr 24–26 | -77.5 | -56.7 | -72.3 | -60.4 |
| May 8-10 | -77.5 | -58.0 | -72.4 | -59.3 |
| May 9-12 | -77.7 | -58.5 | -72.1 | -60.5 |
| May 16-19 | -77.5 | -57.3 | -72.3 | -59.2 |
| May 27–28 | -77.5 | -56.9 | -72.2 | -62.2 |
| May 28-30 | -74.9 | -55.8 | -74.0 | -59.7 |
| Jun 2-5 | -77.7 | -55.0 | -72.4 | -65.9 |
| Jun 9-12 | -75.3 | -56.9 | -74.0 | -67.0 |
| Jun 13-14 | -77.4 | -55.0 | -72.2 | -65.0 |
| Jun 16 | -77.4 | -55.9 | -72.3 | -62.0 |
| Jun 21 | -69.9 | -54.2 | -59.8 | -58.9 |
| Jun 26-27 | -78.6 | -62.0 | -73.5 | -70.1 |

Note 1 – All dates are in 1993.

Note 2 – "Global" longitude ranges are -79.8 to -54.0 and -74.6 to -63.6.

| Table 8 | S — SAMAS | Gulf | Stream | Mean | Position | Errors |
|---------|-----------|------|--------|------|----------|--------|
|---------|-----------|------|--------|------|----------|--------|

| Date | Global 1 | Global 2 | Special 1 | Special 2 |
|--------------|----------|----------|-----------|-----------|
| Mar 8-12 | 90.9 | 44.5 | 50.2 | 50.4 |
| Mar 12–16 | 237.4 | 99.6 | 148.5 | 80.2 |
| Mar 21-23 | 69.6 | 59.7 | 83.7 | 50.8 |
| Mar 28-31 | 43.2 | 59.3 | 45.7 | 70.5 |
| Mar 31-Apr 4 | 103.3 | 17.9 | 26.8 | 22.5 |
| Apr 7–11 | 56.6 | 96.9 | 69.2 | 92.3 |
| Apr 18–20 | 44.0 | 42.2 | 58.4 | 59.4 |
| Apr 20–24 | 50.6 | 18.8 | 58.1 | 19.5 |
| Apr 24–26 | 56.5 | 35.9 | 64.9 | 67.2 |
| May 8-10 | 54.9 | 53.5 | 61.1 | 56.4 |
| May 9–12 | 45.1 | 16.0 | 15.0 | 15.7 |
| May 16-19 | 30.6 | 29.5 | 40.9 | 41.9 |
| May 27–28 | 67.0 | 18.6 | 49.6 | 24.2 |
| May 28–30 | 26.1 | 13.8 | 20.1 | 12.6 |
| Jun 2-5 | 75.0 | 26.0 | 49.7 | 17.3 |
| Jun 9-12 | 32.2 | 22.7 | 31.2 | 17.0 |
| Jun 13-14 | 98.1 | 12.8 | 90.1 | 13.0 |
| Jun 16 | 69.9 | 11.9 | 56.7 | 17.6 |
| Jun 21 | 90.6 | 161.6 | 112.8 | 41.3 |
| Jun 26-27 | 58.4 | 66.6 | 57.0 | 86.4 |
| Mean | 70.00 | 45.39 | 59.49 | 42.81 |
| Std. Dev. | 45.21 | 38.03 | 31.33 | 26.64 |

Note 1 - All dates are in 1993.

Note 2 - Column headings for position errors refer to longitude ranges used in calculations.

Note 3 - Position errors are in kilometers.

in those two columns are judged to be more reliable. It is probably best to ignore the other two columns.

4.0 CONCLUSIONS

This study quantifies the feasibility of automated analysis of satellite imagery reported by Holyer and Peckinpaugh (1990) by testing SAMAS on a large data set and providing a statistical analysis of the results. SAMAS 1.2 found over 80% of the rings the human expert found, with a mean position error of approximately 22 km and a mean fractional size error of 0.165. These figures compare favorably with those reported for the earlier version of SAMAS (Holyer and Peckinpaugh 1990). This study also presents quantitative information on the accuracy of Gulf Stream North Wall location for the first time. Gulf Stream mean position errors were in the range of 40–45 km.

5.0 ACKNOWLEDGMENTS

Thanks are extended to Bobby Grant of Sverdrup Technology, Inc. for his work processing the data and figure preparation. This work was sponsored by the Space and Naval Warfare Systems Command, CDR D. Markham, Program Manager, under Program Element 0603207N.

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